vents shows that EC is 5.7 times more difficult to displace from the cation than is ODCB. This involves the assumption that there is not much difference in the free energy of interaction of TPPO with the solvents EC and ODCB themselves. Grunwald and Miller ${ }^{17}$ have recently reported that Henry's law constant, a measure of solute-solvent interaction, for benzyl chloride as solute increased by a factor of 4.6 in going from dioxane as solvent to ethanol. With this in mind, we still believe that the relative magnitudes of the free energies of interaction of solvent and ligand with the cation play the major role in determining the values of $K_{\mathrm{L}}$ we report here. Comparison of these with the ion-pair dissociation constants for methyltri- $n$-butylammonium perchlorate in the two solvents EC and ODCB is instructive in this regard. The ratio, $K$ (in EC) $/ K($ in ODCB $)$, is 15.4 for the perchlorate. Treating the ion-pair dissociation process in a manner analogous to that employed for the cation complex, then we may write

$$
\begin{equation*}
\mathrm{A}^{+}, \mathrm{X}^{-}+n \mathrm{~S} \rightleftharpoons \mathrm{~A}^{+}, \mathbf{S}_{n+}+\mathrm{X}^{-}, \mathbf{S}_{n-} ; n=n_{+}+n_{-} \tag{9}
\end{equation*}
$$

where $n$ is the number of specifically solvating solvent molecules added to the ions in the pair dissociation process. The free ions are more stable in EC by a factor of 15.9 . If we assume that the stability of the pairs is the same in the two solvents, and that the relative stability of the cation in EC to that in ODCB is given by the inverse ratio of the $K_{\mathrm{L}}$ values found in this work, then the cation is more stable by a factor of 5.7, leaving a factor of 2.8 for the increase in the stability of the perchlorate anion in EC over that in ODCB. That the cation-solvent interaction should play a greater role in these solvents is reasonable since both solvent molecules have the negative ends of their dipoles more unprotected and available for ionsolvent interaction than are the positive ends of the dipoles. The value of the ratio of the ion-pair dissociation constants in these two solvents, $K(\mathrm{EC}) / K$ (ODCB), is very sensitive to the nature of the cation, and less sensitive to the nature of the anion. The ratio for tri-n-
butylammonium picrate has been found ${ }^{1}$ to be 71 , while that for the tetra- $n$-butylammonium picrate has been reported ${ }^{10}$ as 13.2 . The ratio for tetra- $n$-butylammonium nitrate is ${ }^{10} 25.6$.

Ramsey and co-v/orkers ${ }^{13}$ argue that this effect, the increased dissociation of many salts in EC compared to other solvents having almost the same dielectric constant, is due to an increase in the dielectric constant in the neighborhood of the ions in EC, charged species favoring the gauche form of ethylene chloride. Whatiner one chooses to view the effect in terms of an increased local dielectric constant in EC, or in terms of increased specific ion-solvent interaction, is a matter of taste. We prefer the latter description since it leads ${ }^{1}$ to consideration of another solvent parameter, the vapor pressure, in addition to dielectric constant (and dipole moment), which should be of value in accounting for the "solvating power" of a solvent. The greater the escaping tendency (the vapor pressure) of solvent molecules from solvent, the more negative the free energy of specific solvation as in eq. 9. Beard and Plesch recently ${ }^{18}$ found that the ion-pair dissociation constant for methyltriethylammonium iodide in methylene chloride did not decrease as much with increasing temperature as would be required by the corresponding decrease in the $D T$ product, eq. 2. They explained their results in terms of a decrease in the distance of closest approach, $a$, as the temperature increases. The decrease in $a$ is explained as being due to a decrease in pair-solvent interaction as the temperature increases. We offer the alternative explanation that increased specific ion-solvent interaction is occurring upon dissociation of the pair and as the temperature increases, the vapor pressure and thus the solvating power of methylene chloride increases, leading to a smaller decrease in $K$ with rising temperature than one would expect solely from the change in the $D T$ product in eq. 2.

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(18) J. H. Beard and P. H. Plesch, J. Chem. Soc., 4879 (1964).

# Calculation of Chemical Shifts. III. Trivalent Phosphorus ${ }^{1}$ 

H. S. Gutowsky and John Larmann ${ }^{2}$<br>Contribution from the Noyes Chemical Laboratory, University of Illinois, Urbana, Illinois. Received April 14, 1965

Expressions are developed for the isotropic, paramagnetic contribution $\sigma_{A}{ }^{(2)}$ to the magnetic shielding of group $V$ nuclei in $A X_{3}$ molecules, and for the anisotropy of the paramagnetic shielding tensor. The localized molecular orbital treatment employs hybridization and ionicity as bond parameters. A comparison of the ${ }^{31} P$ shifts ob-
served in $\mathrm{PH}_{3}, P\left(\mathrm{CH}_{3}\right)_{3}$, and the phosphorus trihalides with values calculated for $\sigma^{(2)}$ shows that differences in the latter account for the major features of the observed shifts. Also, the calculations indicate that the variations in $\sigma^{(2)}$ do not depend solely upon changes in any one bond parameter.
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(2) National Institutes of Health postdoctoral fellow.

## I. Introduction

Theoretical studies ${ }^{3,4}$ of chemical shifts indicate that for all but the very light nuclei ${ }^{4}$ the dominant contribution to the nuclear shielding tensor is $\sigma^{(2)}$, the second-order paramagnetic term for the atom in question. Expressions for $\boldsymbol{d}^{(2)}$ in terms of orbital populations were developed by Pople ${ }^{5}$ and by Karplus and Das. ${ }^{6}$ More recently, this type of formulation was extended ${ }^{4}$ to include $d$ - as well as p-orbitals, and the results were used to analyze the xenon chemical shifts ${ }^{7}$ observed in some of the new xenon fluorides. The method is limited by its approximate nature and by the fact that there are usually several more adjustable parameters in the theory than there are observable quantities. But its relative simplicity is attractive, so we have explored further the extent to which the differences calculated for $\boldsymbol{d}^{(2)}$ can account for the general trends observed in chemical shifts. In particular, we consider here the ${ }^{31} \mathrm{P}$ shifts reported some years ago for a variety of trivalent phosphorus compounds. ${ }^{8-10}$

Two attempts have been made to relate the ${ }^{31} \mathrm{P}$ chemical shifts in trivalent phosphorus compounds to differences in the second-order paramagnetic term. In the first, ${ }^{9}$ the "p-electron unbalance" at the ${ }^{31} \mathrm{P}$ nucleus was expressed simply as the vector sum of contributions from the phosphorus bonding orbitals, each of which was taken to be of the form, including bond ionicity, employed for the ${ }^{19} \mathrm{~F}$ shifts. ${ }^{3}$ Later, this was modified ${ }^{11}$ by adjusting the p-electron unbalance to particular values for the limiting cases of $\mathrm{p}^{3}$ - and $\mathrm{sp}^{3}$-hybridization. However, neither approach is consistent with the general formulation for $\mathbf{0}^{(2)}$. Therefore, we have used the previous derivation ${ }^{4-6}$ of the components of $\mathbf{d}^{(2)}$ to obtain appropriate expressions for the isotropic shielding $\sigma_{A}{ }^{(2)}$ of the A nucleus in pyramidal, sphybridized, $\mathrm{AX}_{3}$ compounds as well as for the anisotropy $\eta_{\sigma}{ }^{(2)}$, in terms of localized bond parameters. These results are then applied to the ${ }^{31} \mathrm{P}$ shifts observed in some typical compounds.

## II. $\boldsymbol{o}_{\mathrm{A}(2)}$ in $\mathrm{AX}_{3}$ Pyramidal Compounds

In this section, $\boldsymbol{\sigma}^{(2)}$ is obtained in analytical form applicable to group $V$ elements in trivalent compounds for which $\pi$-bonding is negligible. The wave functions of the valence electrons centered on A are assumed to be hybrids, composed of $s$ - and p-orbitals of the following form.

$$
\begin{align*}
\sigma_{\mathrm{X}} & =N_{\mathrm{X}}\left(\mathrm{~s}+\lambda_{\mathrm{X}} \mathrm{p}_{i}\right)  \tag{1}\\
\sigma_{\mathrm{lp}} & =N_{\mathrm{lp}}\left(\mathrm{~s}+\lambda_{\mathrm{lp}} \mathrm{p}_{j}\right) \tag{2}
\end{align*}
$$

Here, $\sigma_{\mathrm{X}}$ is the hybrid orbital directed toward atom X ; $N_{\mathrm{X}}$ is the normalization constant, which is related to the per cent " $s$ " character by $\%$ " $s$ " $=100 N_{\mathrm{X}}{ }^{2}$; $\lambda_{\mathrm{x}}$ is the hybridization mixing coefficient; and $p_{i}$ is a $p-$ orbital directed toward the $X$ atom. Similar definitions apply to the lone-pair hybrid, $\sigma_{\mathrm{lp}}$. This formulation
(3) A. Saika and C. P. Slichter, J. Chem. Phys., 22, 26 (1954).
(4) C. J. Jameson and H. S. Gutowsky, ibid., 40, 1714 (1964).
(5) J. Pople, Proc. Roy. Soc. (London), A239, 541, 550 (1957).
(6) M. Karplus and T. P. Das, J. Chem. Phys., 34, 1683 (1961)
(7) C. J. Jameson and H. S. Gutowsky, ibid., 40, 2285 (1964).
(8) H. S. Gutowsky and D. W. McCall, ibid., 22, 162 (1954).
(9) N. Muller, P. C. Lauterbur, and J. Goldenson, J. Am. Chem. Soc., 78, 3557 (1956).
(10) J. R. Van Wazer, C. F. Callis, J. N. Shoolery, and R. C. Jones, ibid., 78, 5715 (1956).
(11) J. R. Parks, ibid., 79, 757 (1957).
assumes that the internuclear and interorbital angles are identical. Such may not be the case, but in the absence of definitive evidence to the contrary it is a reasonable assumption.

The orbital parameters $N_{\mathrm{X}}, \lambda_{\mathrm{X}}, N_{\mathrm{lp}}$, and $\lambda_{\mathrm{lp}}$ are then determined by the molecular geometry. A necessary and sufficient condition for the orthogonality of two hybrid orbitals, $s+\lambda p_{i}$ and $s+\mu p_{j}$, has been stated by Coulson ${ }^{12}$ to be

$$
\begin{equation*}
1+\lambda \mu \cos \theta_{i j}=0 \tag{3}
\end{equation*}
$$

where $\theta_{i j}$ is the interorbital angle. This relationship, along with bond angle data and geometrical considerations, enables one to determine all of the orbital parameters.

The $\sigma_{\mathrm{x}}$ hybrid on A may be combined with a bonding orbital of the X atom to give a doubly occupied localized molecular orbital of the form

$$
\begin{array}{r}
\psi_{\mathrm{AX}}=\left\{2\left[1+\left(1-i_{\mathrm{X}}{ }^{2}\right)^{1 / 2} S_{\mathrm{X}}\right]\right\}^{-1 / 2}\left[\left(1-i_{\mathrm{X}}\right)^{1 / 2} \sigma_{\mathrm{X}}+\right. \\
\left.\left(1+i_{\mathrm{X}}\right)^{1 / 2} \phi_{\mathrm{X}}\right] \tag{4}
\end{array}
$$

for $\mathrm{A}-\mathrm{X}$ bonds, and

$$
\begin{equation*}
\psi_{1 \mathrm{p}}=\sigma_{\mathrm{lp}} \tag{5}
\end{equation*}
$$

for the A atom's lone pair. The parameter $i_{\mathrm{X}}$, where $0 \leq i_{\mathrm{X}} \leq 1$, is a measure of the ionicity of the $\mathrm{A}-\mathrm{X}$ bond; $\phi_{\mathrm{X}}$ is the bonding orbital on atom X and may be a hybrid type; and $S_{\mathrm{X}}$ is the overlap between $\sigma_{\mathrm{X}}$ and $\phi \mathrm{x}$.

For molecules without d-orbital bonding, the diagonal elements $\sigma_{\alpha \alpha}{ }^{(2)}$ of $\mathbf{0}^{(2)}$ were found to be of the form ${ }^{4-6}$

$$
\begin{equation*}
\sigma_{\alpha \alpha}^{(2)}=-\left(e^{2} \hbar^{2} / \Delta m^{2} c^{2}\right)\left\langle 1 / r^{3}\right\rangle_{\mathrm{p}} P_{\alpha \alpha} \tag{6}
\end{equation*}
$$

where $\Delta$ is the average excitation energy and $\left\langle 1 / r^{3}\right\rangle_{p}$ is the average value of $r^{-3}$ for the p-electrons in the valence shell of A . The quantity $P_{\alpha \alpha}$ is given in Appendix A of ref. 4 in terms of the orbital populations $\mathrm{p}_{\alpha \alpha}$ which are defined in eq. 2 of the same paper. The contribution of $\delta^{(2)}$ to the isotropic shielding, which governs the high resolution n.m.r. spectra of liquids and gases, is

$$
\begin{equation*}
\sigma^{(2)} \equiv \sigma_{\mathrm{av}}^{(2)}=\frac{1}{3}_{\alpha} \sigma_{\alpha \alpha^{(2)}} \tag{7}
\end{equation*}
$$

The anisotropy of $\boldsymbol{\delta}^{(2)}$ may be defined as

$$
\begin{equation*}
\eta_{\sigma}{ }^{(2)}=\sigma_{z z}{ }^{(2)}-\frac{1}{2}\left(\sigma_{x x}{ }^{(2)}+\sigma_{y y}{ }^{(2)}\right) \tag{8}
\end{equation*}
$$

when the nucleus in question is on the $z$ axis which is threefold or higher in symmetry.

In order to apply eq. 6-8 to the wave functions in eq. $1-5$, we place the $A$ atom at the origin of cartesian coordinates, with $\sigma_{1 \mathrm{p}}$ along the $z$ axis and one of the $\sigma_{\mathrm{X}}$ orbitals in the $x z$ plane. The vectorial nature of p-orbitals is used to express the $\mathrm{p}_{i}$ and $\mathrm{p}_{j}$ of eq. 1 and 2 in terms of the $\mathrm{p}_{x}-, \mathrm{p}_{y}-$, and $\mathrm{p}_{z}$-orbitals. Thereby, the following general equations are obtained for the orbital populations in terms of the bond parameters

$$
\begin{equation*}
\mathrm{p}_{x x}=\mathrm{p}_{y y}=4 N_{\mathrm{X}}{ }^{2} \lambda_{\mathrm{X}} I_{\mathrm{X}^{2}} \sin ^{2} \frac{\theta}{2} \tag{9}
\end{equation*}
$$

(12) C. A. Coulson, "Valence," Oxford University Press, New York, N. Y., 1952, p. 194.

Table I. Summary of Structural ${ }^{a}$ and Bond Parameters Used in Calculating ${ }^{31} \mathrm{P}$ Chemical Shifts for $\mathrm{PX}_{3}$ Molecules

| X | $r_{\mathrm{P}-\mathrm{X},}$, <br> $\AA$. | $\angle \mathrm{XPX}$, <br> deg. | $N_{\mathrm{X}}$ | $\lambda_{\mathrm{x}}$ | $N_{\mathrm{lp}}$ | $\lambda_{\mathrm{ip}}$ | $i_{\mathrm{X}}$ | $I_{\mathrm{X}}{ }^{2}$ | $\Delta$, <br> e.v. |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H | 1.42 | 93.3 | 0.223 | 4.37 | 0.923 | 0.419 | 0.00 | 0.309 | 8 |
| $\mathrm{CH}_{3}$ | 1.87 | 100 | 0.385 | 2.40 | 0.746 | 0.893 | 0.07 | 0.295 | 8 |
| F | 1.52 | 104 | 0.441 | 2.03 | 0.645 | 1.19 | 0.40 | 0.288 | 7.5 |
| Cl | 2.00 | 101 | 0.400 | 2.29 | 0.721 | 0.962 | 0.15 | 0.281 | 6 |
| Br | 2.23 | 100 | 0.385 | 2.40 | 0.746 | 0.893 | 0.10 | 0.301 | 6 |
| I | 2.47 | 98 | 0.349 | 2.61 | 0.804 | 0.740 | 0.05 | 0.317 | 6 |

a J. Van Wazer, "Phosphorus and Its Compounds," Vol. I, Interscience Publishers, Inc., New York, N. Y., 1958, pp. 181, 222.

$$
\begin{equation*}
\mathrm{p}_{z z}=2 N_{\mathrm{X}}{ }^{2} \lambda_{\mathrm{X}}{ }^{2} I_{\mathrm{X}}{ }^{2}\left(3-4 \sin ^{2} \frac{\theta}{2}\right)+2 N_{\mathrm{lp}}^{2} \lambda_{\mathrm{pp}}^{2} \tag{10}
\end{equation*}
$$

where $\theta$ is the $\mathrm{X}-\mathrm{A}-\mathrm{X}$ bond angle, and

$$
\begin{equation*}
I_{\mathrm{X}}{ }^{2}=\frac{\left(1-i_{\mathrm{X}}\right)}{2\left[1+\left(1-i_{\mathrm{X}}\right)^{1 / 2} S_{\mathrm{X}}\right]} \tag{11}
\end{equation*}
$$

Introduction of eq. 9 and 10 for the orbital populations into the equations ${ }^{4}$ for $\sigma_{\alpha \alpha}{ }^{(2)}$ leads to

$$
\begin{array}{r}
\sigma^{(2)}=-\left(2 e^{2} \hbar^{2} / 3 \Delta m^{2} c^{2}\right)\left\langle 1 / r^{3}\right\rangle_{\mathrm{p}}\left[6 N_{\mathrm{X}}{ }^{2} \lambda_{\mathrm{X}}{ }^{2} I_{\mathrm{X}}{ }^{2}+\right. \\
2{N_{\mathrm{lp}}{ }^{2} \lambda_{\mathrm{lp}}{ }^{2}-24 N_{\mathrm{X}}{ }^{4} \lambda_{\mathrm{X}}{ }^{4} I_{\mathrm{X}}{ }^{4}\left(\sin ^{2} \frac{\theta}{2}-\sin ^{4} \frac{\theta}{2}\right)-}^{\left.8 N_{\mathrm{X}}{ }^{2} \lambda_{\mathrm{X}}{ }^{2} N_{\mathrm{lp}^{2}}{ }^{2} \lambda_{\mathrm{lp}}{ }^{2} \sin ^{2} \frac{\theta}{2}\right]}
\end{array}
$$

and

$$
\begin{align*}
& \eta_{\sigma}{ }^{(2)}=\left(e^{2} \hbar^{2} / \Delta m^{2} c^{2}\right)\left\langle 1 / r^{3}\right\rangle_{\mathrm{p}}\left[6 N_{\mathrm{X}} \lambda_{\mathrm{X}}{ }^{2} I_{\mathrm{X}}{ }^{2} \times\right. \\
& \quad\left(1-2 \sin ^{2} \frac{\theta}{2}\right)+2 N_{\mathrm{lp}_{\mathrm{p}}}{ }^{2} \lambda_{\mathrm{lp}_{\mathrm{p}}}{ }^{2}+24 N_{\mathrm{X}}{ }^{4} \lambda_{\mathrm{X}}{ }^{4} I_{\mathrm{X}}{ }^{4} \times \\
& \left.\left(2 \sin ^{4} \frac{\theta}{2}-\sin ^{2} \frac{\theta}{2}\right)-8 N_{\mathrm{X}}{ }^{2} \lambda_{\mathrm{X}}{ }^{2} I_{\mathrm{X}}^{2} N_{\mathrm{lp}^{2}} \lambda_{\mathrm{lp}_{\mathrm{p}}} \sin ^{2} \frac{\theta}{2}\right] \tag{13}
\end{align*}
$$

It should be noted that as before ${ }^{4,6}$ these expressions neglect contributions from orbitals centered on atoms other than A. Also, eq. 12 and 13 are unlike the analogous results for the xenon fluorides ${ }^{7}$ in that the extent of sp-hybridization is a directly adjustable parameter by means of the $\mathrm{X}-\mathrm{A}-\mathrm{X}$ interorbital angle $\theta$. It has been assumed that the three $\mathrm{A}-\mathrm{X}$ bonds are equivalent; however, the expressions appropriate for dissimilar substituents are readily obtained though they are algebraically more complex.

## III. Application to ${ }^{31} \mathrm{P}$ Chemical Shifts in Trivalent Compounds

As noted in the Introduction, several structural and bond parameters appear in eq. 12 and 13 for $\sigma^{(2)}$ and $\eta_{\sigma}{ }^{(2)}$. Some of them are directly measurable and thus are available to good accuracy, but others must be estimated in one way or another. Therefore, quantitative tests of chemical shift theory are seldom possible, and this work is no exception. In Table I the various quantities required to calculate $\sigma^{(2)}$ and $\eta_{\sigma}{ }^{(2)}$ are summarized. We have sought to obtain accurate values of these quantities for the six phosphorus compounds treated, and the results are listed in the table. In Table II, we give the corresponding values for $\sigma^{(2)}$ and $\eta_{\sigma}{ }^{(2)}$, and the differences in $\sigma^{(2)}$ are then compared with the observed ${ }^{31} \mathrm{P}$ chemical shifts.

Table II. Summary of Values Calculated for the ${ }^{34} \mathrm{P} \sigma^{(2)}$ and $\eta \sigma^{(2)}$ (in p.p.m.) and Comparison with Observed Chemical Shifts for Several Trivalent Phosphorus Compounds

| Compound | $\sigma^{(2)}$ | $\eta_{\sigma}{ }^{(2)}$ | $\Delta \sigma^{(2)}$ | $\delta^{a}$ |
| :--- | ---: | ---: | ---: | ---: |
| $\mathrm{PH}_{3}$ | -570 | 50 | 293 | 465 |
| $\mathrm{P}\left(\mathrm{CH}_{3}\right)_{3}$ | -630 | 162 | 233 | 289 |
| $\mathrm{PF}_{3}$ | -709 | 238 | 154 | 130 |
| $\mathrm{PI}_{3}$ | -823 | 146 | 40 | 49 |
| $\mathrm{PCl}_{3}$ | -852 | 254 | 11 | 8 |
| $\mathrm{PBr}_{3}$ | -863 | 207 | 0 | 0 |

${ }^{a}$ From ref. 8 and 9 , with the zero of reference changed from $\mathrm{H}_{3} \mathrm{PO}_{4}$ to $\mathrm{PBr}_{3}$. A larger positive number corresponds to an upfield shift.

Parameters Required to Evaluate $\sigma^{(2)}$ and $\eta_{\sigma}{ }^{(2)}$. As indicated in II, the interorbital angle $\theta$ is taken to be the experimental $\mathrm{X}-\mathrm{P}-\mathrm{X}$ bond angle. Also, this angle establishes the values given in Table I for the $N$ and $\lambda$ values. The quantity $I_{\mathrm{X}}{ }^{2}$ contains the ionic character $i_{\mathrm{X}}$ and the overlap $S_{\mathrm{X}}$ between the bonding orbital on atom X and that on phosphorus. The overlap was evaluated using standard sources of overlap integrals ${ }^{13,14}$ and the experimental $\mathrm{P}-\mathrm{X}$ bond distance. The factor $i_{\mathrm{X}}$ is more important and more difficult to assess. A simple empirical formula used for diatomic molecules ${ }^{15}$ is

$$
\begin{equation*}
i_{\mathrm{X}}=0.16\left(x_{\mathrm{A}}-x_{\mathrm{B}}\right)+0.035\left(x_{\mathrm{A}}-x_{\mathrm{B}}\right)^{2} \tag{14}
\end{equation*}
$$

where $x_{\mathrm{A}}$ and $x_{\mathrm{B}}$ are the Pauling electronegativities. The values of $i_{\mathrm{X}}$ in Table I were estimated with this formula; they will be somewhat large for the corresponding polyatomic bond. However, the values obtained should be reasonable upper bounds for $i_{\mathrm{X}}$, and give lower bounds for $I_{\mathrm{X}}{ }^{2}$.

As usual, the average electronic excitation energy $\Delta$ presents the most difficulty and probably is the least certain of the required parameters. The ultraviolet spectra of the molecules considered here are of the predissociation type with long ranges of continuous absorption which make it somewhat difficult to assign the appropriate frequencies necessary for determining $\Delta$. The values of $\Delta$ were obtained by an arithmetic averaging of the energy bands reported for these molecules and are discussed in detail below. Weaker bands were weighted to a lesser degree based on intensity considerations.

[^0]The spectra of phosphine ${ }^{16}$ and trimethylphosphine ${ }^{16 a}$ are similar and $\Delta=8 \mathrm{e} . \mathrm{v}$. is assigned to both compounds. Phosphine has a maximum in its lowest energy band at $1910 \AA ., 6.6$ e.v. A predissociation band has a maximum at $1800 \AA ., 7$ e.v., while at shorter wave lengths the bands all overlap into a continuum that extends downward to $1250 \AA ., 10.1$ e.v. Trimethylphosphine has a band similar to phosphine at $2010 \AA$.; the shorter wave length side to $1850 \AA$. is continuous.

The spectra of $\mathrm{PCl}_{3}, \mathrm{PBr}$, and $\mathrm{PI}_{3}$ are generally similar in appearance and in the positions of maxima; therefore the same $\Delta$, of 6 e.v., is used for all three compounds. As to details, the spectrum of $\mathrm{PCl}_{3}$ has been measured ${ }^{16,17}$ from about 3000 down to $1200 \AA$. At long wave lengths, an absorption band occurs at $2800 \AA$. ., 4.4 e.v., which is attributed to nonbonding transitions. A second maximum occurs at 2170 $\AA$ A., 5.6 e.v., in a band of transitions. Another weaker band starting at $1600 \AA$. with a maximum at 1470 A., 8.3 e.v., has also been observed. The spectra for phosphorus tribromide ${ }^{17}$ and phosphorus triiodide ${ }^{18}$ are much less complete. However, the tribromide has two bands at 2635 A., 4.7 e.v., and 3085 $\AA ., 4.1$ e.v., which correspond to the nonbonding transition in the trichloride. Below $2400 \AA$. the tribromide appears to have a continuous absorption, again similar to the trichloride. Phosphorus triiodide has been measured in solution and has the typical nonbonding band at 2850 A., 4.3 e.v. Thus, to the extent that they have been investigated, the spectra of $\mathrm{PBr}_{3}$ and $\mathrm{PI}_{3}$ are very similar to that of $\mathrm{PCl}_{3}$, so the $\Delta$ for all three molecules is taken to be the trichloride average of 6 e.v.

Phosphorus trifluoride ${ }^{16 \mathrm{~b}}$ has been measured from 2000 down to $1200 \AA$., and has a spectrum similar to the trichloride, except that it is displaced to shorter wave lengths. Two bands appear at 1564 and $1515 \AA$. , about 7.8 e.v. A second, weaker band starts at 1405 $\AA$. with a maximum at $1300 \AA ., 9.2$ e.v. The bands then oyerlap into the typical continuum pattern below $1300 \AA$. At wave lengths longer than $2000 \AA$. the nonbonding transition typical of the trihalides would be expected. This would be expected to lower the value of $\Delta$ to 7.5 e.v.
Finally, we need a value of $\left\langle 1 / r^{3}\right\rangle$ for the 3 pvalence electrons of phosphorus. This may be obtained from experimental values for spin-orbit interactions in the free atom, and in this manner Barnes and Smith ${ }^{19}$ calculated $\left\langle a_{0}{ }^{3} / r^{3}\right\rangle_{3 \mathrm{p}}$ for a series of atoms. Their value for phosphorus is $\left\langle a_{0}^{3} / r^{3}\right\rangle_{3 \mathrm{p}}=3.48$ which we used.

## IV. Results and Discussion

Table II lists the values for $\sigma^{(2)}$ and $\eta_{\sigma}{ }^{(2)}$ obtained from eq. 12 and 13 by means of the parameters summarized in Table I. Also, for purposes of comparison with experiment, the differences between the $\sigma^{(2)}$ calculated for each molecule and for $\mathrm{PBr}_{3}$ are given along with the observed ${ }^{31} \mathrm{P}$ chemical shift referred to $\mathrm{PBr}_{3}$. These calculated variations in $\sigma^{(2)}$ fall in the
(16) (a) M. Halmann, J. Chem. Soc., 2853 (1963); (b) C. M. Humphries, A. D. Walsh, and P. A. Warsop, Discussions Faraday Soc., 35, 148 (1963).
(17) E. Teller and H. Sponer, Rev. Mod. Phys., 13, 75 (1941)
(18) R. Potteril and O. Walker, Trans. Faraday Soc., 33, 363 (1937).
(19) R. G. Barnes and W. V. Smith, Phys. Rev.. 93, 95 (1954).
same order as do the observed chemical shifts, and the numerical agreement is reasonably good considering the approximations inherent in the theory. Also, it should be kept in mind that the experimental errors in bond angles and bond lengths are appreciable and that they affect the results of the calculations.
The $\Delta \sigma^{(2)}$ calculated for $\mathrm{PH}_{3}$ shows the largest deviation from experiment, and that for $\mathrm{P}\left(\mathrm{CH}_{3}\right)_{2}$ is next. Actually, this could reflect in part our choice of $\mathrm{PBr}_{3}$ rather than $\mathrm{PH}_{3}$ as the reference compound for $\Delta \sigma^{(2)}$ and $\delta$. That is, without further data, it is not clear whether the calculations for the phosphorus trihalides or those for $\mathrm{PH}_{3}$ and $\mathrm{P}\left(\mathrm{CH}_{3}\right)_{3}$ are in error or whether errors in both contribute to the discrepancies. Measurements of the ${ }^{31} \mathrm{P}$ chemical shift anisotropy could be very helpful in this context because, as may be seen in Table II, $\eta_{\sigma}{ }^{(2)}$ has a substantially different dependence upon the localized bond parameters, hybridization, and ionicity than does $\sigma^{(2)}$. Moreover, the anisotropy does not suffer from the uncertainties in choosing a zero of reference, as must be done for comparisons of $\sigma^{(2)}$. In any event, the ${ }^{31} \mathrm{P}$ chemical shifts in these trivalent compounds can be attributed largely to differences in $\sigma^{(2)}$. Also, no single parameter appears to dominate $\Delta \sigma^{(2)}$; instead, differences in ionicity, hybridization, and in $\Delta$ all seem to be important.

There are several possible sources of the nonquantitative agreement between the calculations and experiment, with the more obvious ones being errors in $\Delta$, the neglect of the diamagnetic shielding term, and neglect of overlap between the localized molecular orbitals. ${ }^{3-7}$ This overlap between two localized molecular orbitals is considered to be small. It should not be confused with the overlap $S_{\mathrm{X}}$ appearing in the formula for the localized molecular orbital. The $S_{\mathrm{X}}$ overlap is between bonding atomic hybrids within a given twocentered molecular orbital and is always sizable. The estimates of the bond ionicity seem to be a less likely source of error; at least the ${ }^{19} \mathrm{~F}$ chemical shift observed in $\mathrm{PF}_{3}$ is compatible with the $i_{\mathrm{F}}$ of 0.40 used to calculate the ${ }^{31} \mathrm{P}$ shift in the compound. The method used to make the check is the same as that applied to the ${ }^{19} \mathrm{~F}$ shifts in the xenon fluorides. ${ }^{7}$ For fluorine, the expression for $\sigma^{(2)}$ is simply
$\sigma_{\mathrm{F}}{ }^{(2)}=-\left(2 e^{2} \hbar^{2} / 3 \Delta m^{2} c^{2}\right)\left\langle 1 / r^{3}\right\rangle_{\mathrm{F}}\left[1-\left(i_{\mathrm{F}}+s_{\mathrm{F}}\right)\right]$
with symbols as before except for $s_{\mathrm{F}}$ which is the scharacter of the bonding orbital centered on F . If the experimental value of 464 p.p.m. ${ }^{20}$ for $\sigma_{\mathrm{F}}\left(\mathrm{PF}_{3}\right)$ - $\sigma_{\mathrm{F}}\left(\mathrm{F}_{2}\right)$ is attributed to $\Delta \sigma_{\mathrm{F}}{ }^{(2)}$ and the same values are assigned to the other parameters as before, ${ }^{6,7}$ one inds that $i_{\mathrm{F}} \cong 0.40$ which agrees with the value obtained from eq. 14.
The possible effects of $\pi$-character have been neglected in our calculations. However, the $\pi$-bonding should be nil for $\mathrm{PH}_{3}$ and $\mathrm{P}\left(\mathrm{CH}_{3}\right)_{3}$ and could be no more than $10 \%$ for the phosphorus trihalides. ${ }^{21}$ This might account for part of the discrepancy between the $\Delta \sigma^{(2)}$ calculated for the two groups of compounds and
(20) H. S. Gutowsky and C. J. Hoffman, J. Chem. Phys., 19, 1259 (1951).
(21) See, e.g., T. P. Das and E. L. Hahn, "Nuclear Quadrupole Resonance Spectroscopy," Academic Press Inc., New York, N. Y., 1958.
the observed $\Delta \sigma$ but it is hardly the main cause. ${ }^{22}$ Another possibility is the expansion of the phosphorus radial wave function by an amount proportional to the paired-electron density in the phosphorus bonding orbitals. This effect would be greatest for the least ionic $\mathrm{P}-\mathrm{X}$ bonds, and thus it would tend to decrease $\left\langle 1 / r^{3}\right\rangle_{\mathrm{p}}$ and $\sigma^{(2)}$ for $\mathrm{PH}_{3}$ and $\mathrm{P}\left(\mathrm{CH}_{3}\right)_{3}$ as compared to the trihalides, which is in the direction required. The magnitude of the effect is uncertain, but there is some e.s.r. evidence for its existence. ${ }^{23}$

A noteworthy feature of the calculations of $\sigma^{(2)}$ and of the experimental shifts for the trihalides is the "reversal" of the trends in the case of $\mathrm{PI}_{3}$; that is, the ordering is $\mathrm{PF}_{3}, \mathrm{PI}_{3}, \mathrm{PCl}_{3}$, and $\mathrm{PBr}_{3}$. This is a consequence of the fact that altho igh the bond parameters such as ionicity and bond hybridization change monotonically in the usual sequence $\mathrm{F}, \mathrm{Cl}, \mathrm{Br}$, and I , their ef-
(22)- Of course one would expect $\pi$-bond contributions to be more appreciable in the tetravalent compounds $\mathrm{X}_{3} \mathrm{PO}$ and $\mathrm{X}_{3} \mathrm{PS}$.
(23) K. DeArmond, B. B. Garrett, and H. S. Gutowsky, J. Chem. Phys., 42, 1019 (1965).
fects upon $\sigma^{(2)}$ are nonlinear and, in some instances opposed, so that $\sigma^{(2)}$ goes through a minimum for $\mathrm{PBr}_{3}$. The existence of the minimum is evident also in the ${ }^{31} \mathrm{P}$ shifts found in the series of compounds $\mathrm{PCl}_{3}, \mathrm{PBrCl}_{2}, \mathrm{PBr}_{2} \mathrm{Cl}$, and $\mathrm{PBr}_{3}$. In observations at 16.2 Mc. $/ \mathrm{sec}$., their shifts ${ }^{24}$ were found to be 10.5 , 4.3 , and 0.6 p.p.m. upfield with respect to $\mathrm{PBr}_{3}$. Thus, the change produced in $\sigma$ by substitution of a Br for a Cl is $6.2,3.7$, and 0.6 p.p.m. for the first, second, and third Br , respectively, which follow the general pattern for the unmixed trihalides themselves.

The formulation given here is applicable in principle to ${ }^{14} \mathrm{~N}$ or ${ }^{15} \mathrm{~N}$ shifts in trivalent nitrogen compounds. However, few experimental data are available on nitrogen shifts. It would be particularly relevant to the present work if nitrogen shifts could be measured in $\mathrm{NH}_{3}$ as well as in some of the nitrogen trihalides, to establish whether ammonia has a large upfield shift such as that found for ${ }^{31} \mathrm{P}$ in phosphine.
(24) E. Fluck, J. R. Van Wazer, and L. C. D. Groenweghe, J. Am. Chem. Soc., 81, 6363 (1959).

# Silicon-Fluorine Chemistry. II. Silicon-Boron Fluorides ${ }^{1 \mathrm{Ia}}$ 

P. L. Timms, ${ }^{\text {1b }}$ T. C. Ehlert, ${ }^{1 \mathrm{~b}}$ J. L. Margrave, ${ }^{\text {1b }}$ F. E. Brinckman, ${ }^{1 \mathrm{c}}$ T. C. Farrar, ${ }^{\text {1c }}$ and T. D. Coyle ${ }^{1 \mathrm{c}}$<br>Contribution from the Department of Chemistry, Rice University, Houston, Texas, and the National Bureau of Standards, Washington, D. C. Received March 16, 1965

Gaseous $\mathrm{SiF}_{2}$ and $B F_{3}$ are observed to react when condensed together in a trap at liquid nitrogen temperature. Several silicon-boron fuorides have been identified mass spectrometrically, including $S i_{2} B F_{7}, S i_{3} B F_{9}$, and $S i_{4} B F_{11}$. From n.m.r., infrared, and mass spectral data, one concludes that these molecules are members of the homologous series $\operatorname{SiF}_{3}-\left(\mathrm{SiF}_{2}\right)_{n}-\mathrm{BF}_{2}$. The silicon-boron fluorides are thermally stable to at least $200^{\circ}$ as vapors but ignite spontaneously in air. A similar family of mixed fluoro-chloro compounds is obtained by treating $\mathrm{BCl}_{3}$ with $\mathrm{SiF}_{2}$.

It was shown by Pease ${ }^{2}$ that silicon difluoride gas, $\mathrm{SiF}_{2}$, can be conveniently prepared from silicon and silicon tetrafluoride at low pressures and temperatures above $1050^{\circ}$.

$$
\mathrm{Si}(\mathrm{~s})+\mathrm{SiF}_{4}(\mathrm{~g})=2 \mathrm{SiF}_{2}(\mathrm{~g})
$$

Studies in this laboratory have shown ${ }^{3}$ that silicon difluoride is a surprisingly stable gaseous species, although it can be made to react with a wide variety of compounds.

[^1]The molecule $\mathrm{SiF}_{2}$ might act either as an electron donor or acceptor. This would be true if the molecule were in either the triplet or singlet state, since, by analogy with difluorocarbene, ${ }^{4}$ these states are likely to be separated by only a small energy barrier. Thus, it was thought that silicon difluoride should be capable of forming adducts of the type $\operatorname{SiF}_{2}-\mathrm{Y}$ where Y is a strong Lewis acid like boron trifluoride. Difluorocarbene has not been observed to act in this way, probably because the inductive effect of the fluorine limits the availability of the electron pair, but with silicon ( $p \rightarrow \mathrm{~d}$ ) $\pi$-bonding could in part compensate for this.
In addition to being a possible acid-base reaction, the combination of silicon difluoride and boron trifluoride was of interest for two other reasons. First, the B-F and Si-F bond energies are rather similar so that a compound of type $\mathrm{SiF}_{2} \cdot \mathrm{BF}_{3}$ might readily rearrange to $\mathrm{SiF}_{3} \mathrm{BF}_{2}$; and second, it was hoped that this reaction would provide a convenient route to forming simple compounds containing silicon-boron bonds, only a few of which have previously been described (the most recent being $\mathrm{SiBCl}_{5}$ by Massey ${ }^{5}$ ).

## Experimental

Silicon difluoride was prepared from silicon and silicon tetrafluoride at $0.1-0.2 \mathrm{~mm}$. pressure and a temperature of $1150^{\circ}$ as described elsewhere. ${ }^{3}$ Boron
(4) F. W. Dalby, J. Chem. Phys., 41, 2297 (1964).
(5) A. G. Massey and D. S. Urch, Proc. Chem. Soc., 284 (1964).


[^0]:    (13) R. S. Mulliken, C. A. Rieke, D. Orloff, and H. Orloff, J. Chem. Phys., 17, 1248 (1949).
    (14) M. Kotani, A. Amemiya, E. Ishiguro, and T. Kimura, "Tables of Molecular Integrals," Maruzen and Co., Ltd., Tokyo, 1955.
    (15) See ref. 12, p. 134. In ref. 6 it has been suggested that the ionic character scale obtained via quadrupole coupling constants is more appropriate for chemical shift calculations.

[^1]:    (1) (a) Presented in part before the 148 th National Meeting of the American Society, Chicago, I11., Sept. 1964; (b) Rice University; (c) National Bureau of Standards.
    (2) D. C. Pease, U. S. Patents 2,840,588 (June 24, 1958) and 3,032,173 (March 20, 1962) assigned to the Du Pont Co., Wilmington, Del.
    (3) (a) P. L. Timms, R. A. Kent, T. C. Ehlert, and J. L. Margrave, Nature, in press; (b) part I: J. Am. Chem. Soc., 87, 2824 (1965).

